

**The III International Scientific and Technical Conference
«Aeroengines of the XXI century»**



Dynamics of the rotor system, supported by the active magnetic bearings

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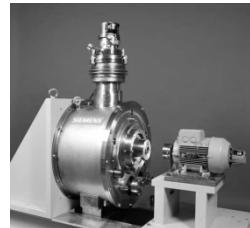
December 2010

Active magnetic bearings

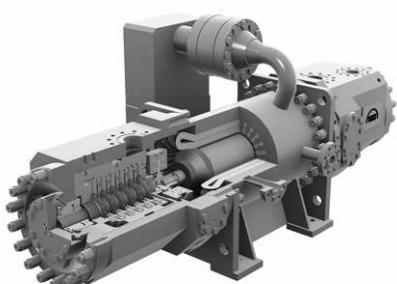
Field of application	Features of application	Problems
<ul style="list-style-type: none">• high-vacuum turbo-molecular pumps• precision measuring instruments, gyroscopes, test desks etc.• centrifugal compressors• grinding and milling spindles• balancing machines• flywheels for energy accumulation• gas generators• pump stations	<ul style="list-style-type: none">• absence of lubrication and wear• absence of contact and contamination• active control of stiffness and damping• rotation speed(up to 800 000 rpm)• low noise level• precision of rotor axis position (up to 0.5 μ m)• work in extreme conditions (high-vacuum, zero gravity, variable temperatures)	<ul style="list-style-type: none">• limited bearing capacity• high objective power• high heat generation• high weight• control system is required



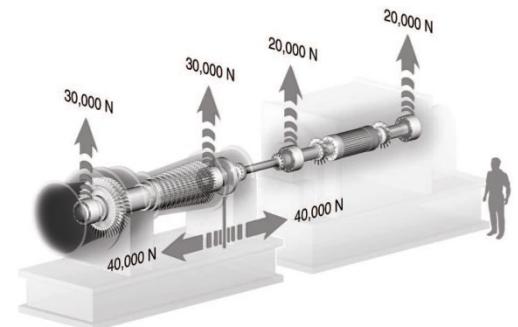
The turbo-blower for cooling a laser (CO_2). Speed is 54000 rpm , the rotor mass is 3.6 kg, the motor power is 12 kW, the radial bearing diameter is 48 mm, the bearing force is 230 N (TRUMPF/MECOS).



The synchronous generator supported by the superconductive magnetic bearings. Temperature is 28K, maximum speed is 4500 rpm (SIEMENS).

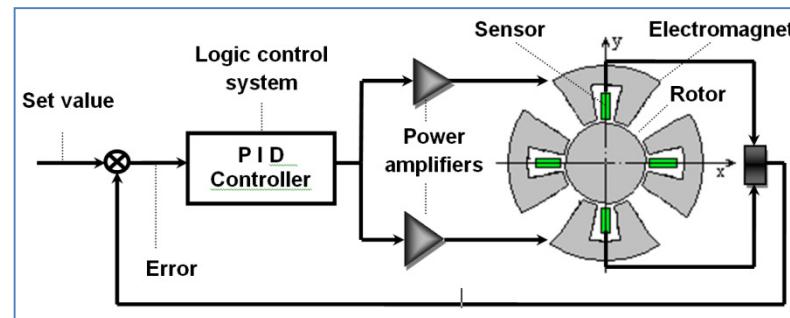
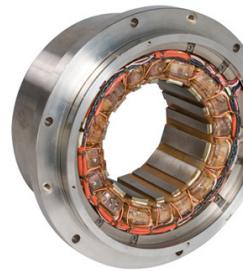


The compressor HOFIM for pumping natural gas: integration of the direct drive and the magnetic bearing in the turbomachine, 6 MW, 9000 rpm (MAN Turbo/S2M).



The gas-turbine generator: 4 radial bearings and 1 thrust bearing, 6010 rpm, 9000 kW, the bearing diameter is 400 mm (S2M).

The modulus – The magnetic bearing – for the rotor dynamics tasks



Magnetic force:

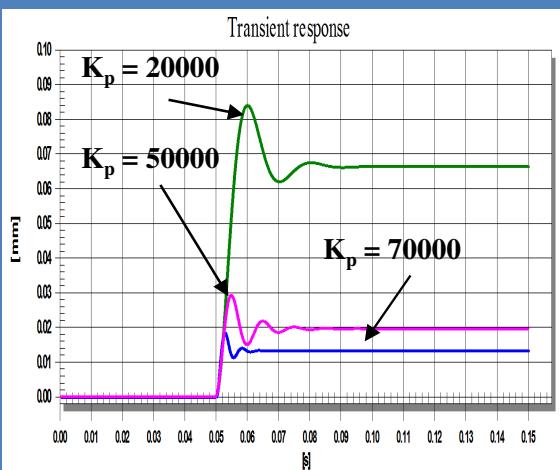
$$F = \frac{\mu_0 N^2 A_\delta}{4} \left(\frac{I_1^2}{(\delta - y)^2} - \frac{I_2^2}{(\delta + y)^2} \right)$$

PID-controller:

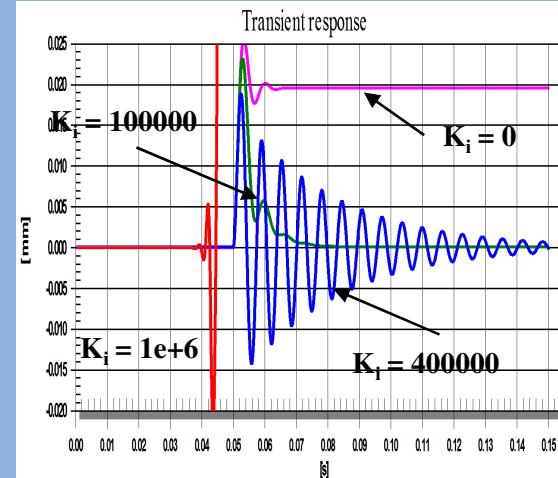
$$I(t) = P + I + D$$

$$I(t) = K_p e(t) + K_i \int_0^t e(t) dt + K_d \frac{de}{dt}$$

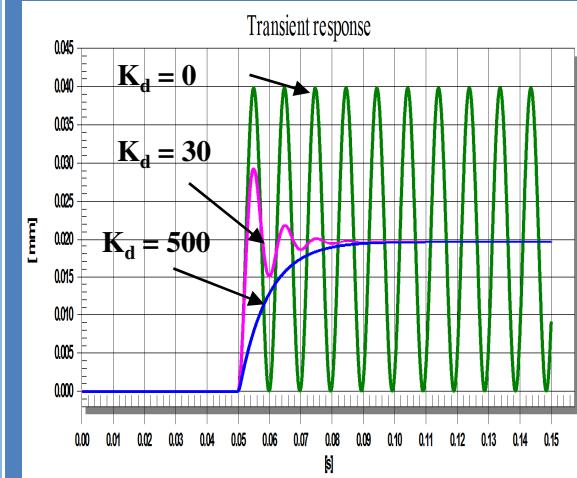
$$\begin{aligned} K_i &= 0 \quad K_d = \text{const} \\ K_p &= \text{var} \end{aligned}$$



$$\begin{aligned} K_p &= \text{const} \quad K_d = \text{const} \\ K_i &= \text{var} \end{aligned}$$



$$\begin{aligned} K_i &= 0 \quad K_p = \text{const} \\ K_d &= \text{var} \end{aligned}$$



The DYNAMICS R4 software for the rotor system analysis and design in the unsteady and non-linear approach

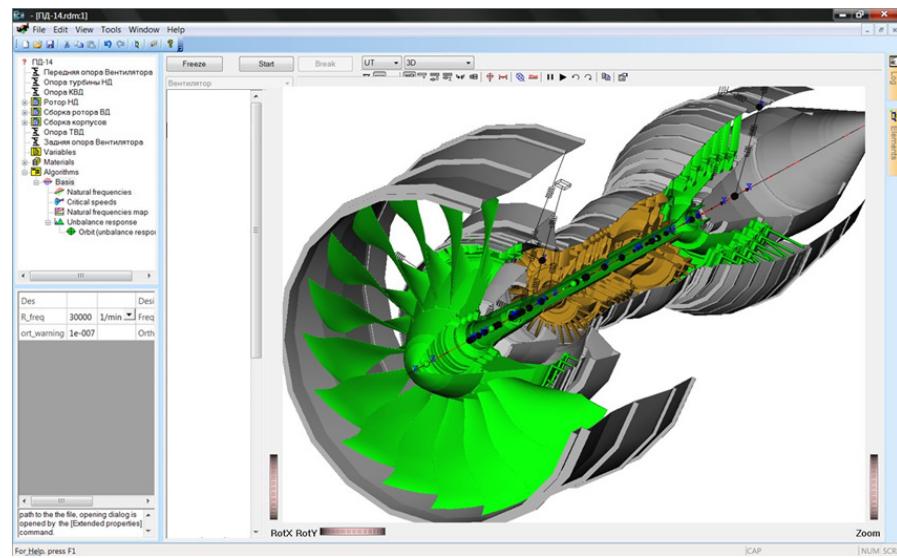


CАТУРН
НПО



DYNAMICS R4

АО „А.Люлька-САТУРН“



Any types of dynamic loads – internal and external– $F(t)$



Dynamic model of the rotor system
Dynamics R4

$$[M]\{\ddot{u}\} + [C]\{\dot{u}\} + [K]\{u\} = \{F(t)\} + \{R\}$$

$\{u\}, \{\dot{u}\}$



$\{R\}$



Model of non-linear link (for example, AMB)

$$\{R\} = K\{u\} + C\{\dot{u}\} + I \int \{u\}$$

$$K = \frac{\mu_0 N^2 A_g I_b}{\delta_0^2} \left(\frac{I_b}{\delta_0} + K_p \right) \quad C = \frac{\mu_0 N^2 A_g I_b}{\delta_0^3} K_d \quad I = \frac{\mu_0 N^2 A_g I_b}{\delta_0^3} K_i$$

The elements for the rotors simulation in Dynamics R4



Spring link

Ball and roller bearings

Deflection limiter (clearance)

Magnetic bearing

Representation
Representation
Representation
Representation

Model
Model
Model
Model

Initial data
Initial data
Initial data
Initial data

Des	Front support	Designation
conn_type	via body	Type of connection
side1_subs	Subsystem 1	Side1 subsystem
side1_l	0	mm side1 offset
side2_subs		Side2 subsystem
trns_exclude	yes	Exclude from transient analysis
Type	Isotropic	Link type
stiff_matrix	...	Stiffness matrix
damp_matrix	...	Damping matrix
d*	0	mm Inner diameter
D*	200	mm Outer diameter
B*	100	mm width

Des	Ball Bearing support 3	Designation
conn_type	via body	Type of connection
side1_subs	Subsystem 1	Side1 subsystem
side1_l	1	mm side1 offset
side2_subs	Subsystem 2	Side2 subsystem
side2_l	1	mm side2 offset
Dr	11.9062	mm Rolling elements diameter
z	11	Rolling elements count
Di	40	mm Inner race diameter
delta1	0	mm Inner race clearance
delta2	0	mm Outer race clearance
Kp_input	input	Type of Hertz stiffness input
Kh	1.334e+010	N/m Hertz stiffness
Cb	2940	N*s/m Damping coefficient
d*	0	mm Inner diameter
D*	0	mm Outer diameter
B*	0	mm width

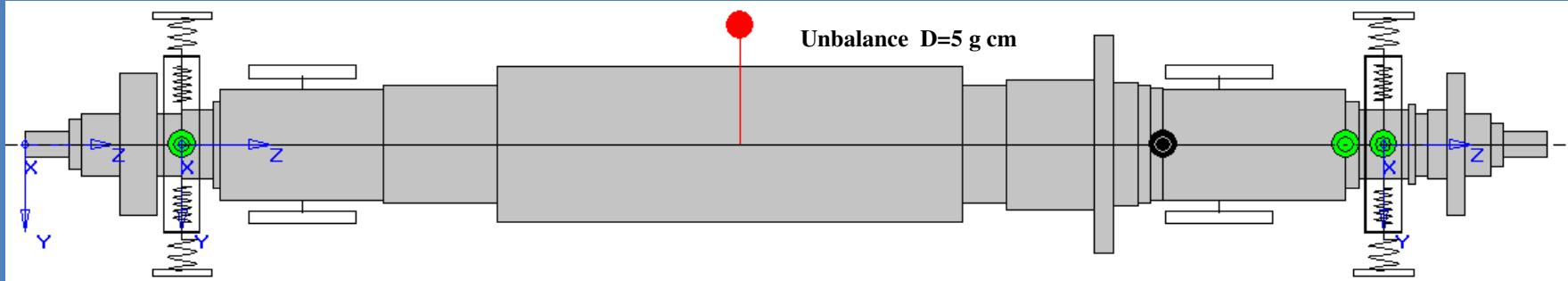
Des	Clearance 2 2	Designation
conn_type	via body	Type of connection
side1_subs	Subsystem 1	Side1 subsystem
side1_l	1	mm side1 offset
side2_subs	Subsystem 2	Side2 subsystem
side2_l	1	mm side2 offset
L1	0	mm Displacement L1
L2	0	mm Displacement L2
L3	0	mm Displacement L3
K1	1600	N/m Damper package 1 stiffness
c1	0	N*s/m Package 1 damping
k2	1e+010	N/m Damper package 2 stiffness
c2	0	N*s/m Package 2 damping
R	50	mm Packet radius
delta	1	mm Radial clearance
e1	0	mm Assembly eccentricity 1
e2	0	mm Assembly eccentricity 2
Teta1	0	deg Initial angle position of e1
Teta2	0	deg Initial angle position of e2
mue	0	Ns/m ² Friction coefficient
Vsmin	0.001	Minimal slipping speed
d*	0	mm Inner diameter
D*	5	mm Outer diameter
B*	0	mm width

Des	AMT1	Название
conn_type	via body	Тип подключения
side1_subs	Подсистема 1	Подсистема для сечения 1 связи
side1_l	155.316	мм положение граничного сечения 1 связи
side2_subs		Подсистема для сечения 2 связи
Type	Изотропный	Тип связи
Opt.Type	стандарт	Режим ввода параметров
Geometry Type	Цилиндр	Тип подшипника
dL	63	мм внутренний диаметр слева
D	220	мм внешний диаметр
b	70	мм Диаметр пакета стали
gap	0.4	мм Радиальный зазор между статором и ротором
Imax	5	A максимальный ток в обмотке
Np	16	Число полюсов электромагнитов
Ncp	4	Число полюсов управления
Teta_CPI	0	deg Угол поворота первого полюса управления
Cooling	полное заполнение паза	Тип обмотки
Flux direction	поперечное	Направление магнитного потока
Jmax	6	A/mm ² Максимальная плотность тока в обмотке
Controller	ПД - регулятор	Тип регулятора
Kp	50000	Пропорциональная составляющая ПД-регул.
Kd	5	Дифференциальная составляющая ПД-регул.
d*	0	мм Внутренний диаметр
D*	0	мм Наружный диаметр
B*	0	мм ширина

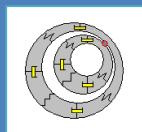
The rotor model on magnetic suspension in Dynamics R4



TRANZIT

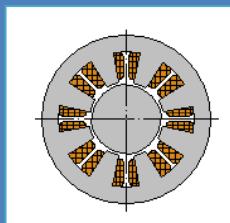


Clearance



Ball bearing

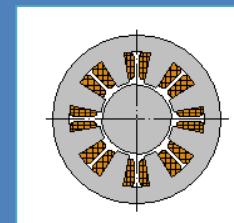
AMB



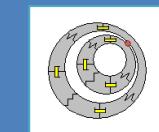
Rotor parameters

Mass, m	23.76 kg
Length, L	852 mm
Moment of inertia, J_d	0.92 kg m²
Nominal speed, ω	500 Hz

AMB



Clearance

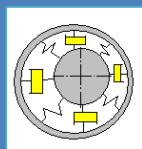


Ball bearing

AMB parameters

Nominal stiffness, N/m	0.5e +8
Nominal damping, N sec/m	6000
Radial clearance, mm	0.5

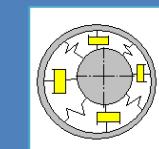
Spring link with the base



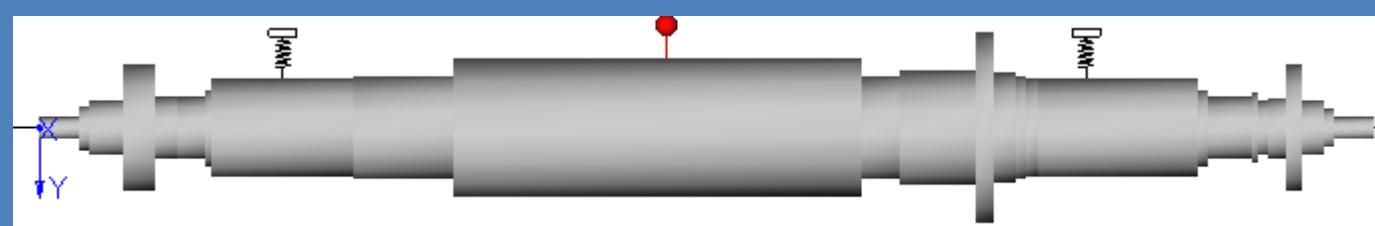
Backup bearings parameters

Stiffness, N/m	1e+8
Damping, N s/m	800
Radial clearance, mm	0.25

Spring link with the base



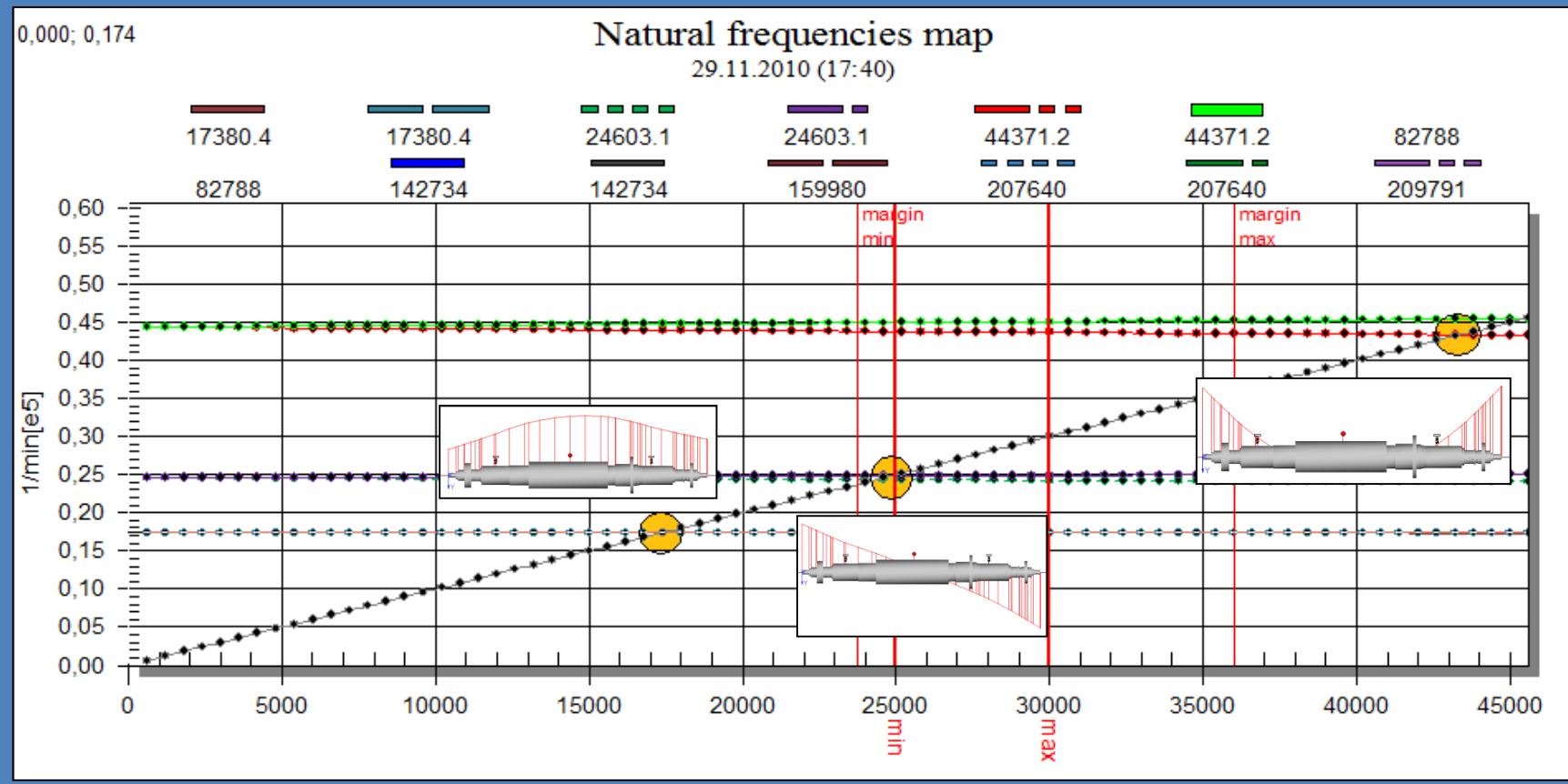
Critical speeds of the rotor supported by AMB



$k_1 = 0.5e +8 \text{ H/m}$

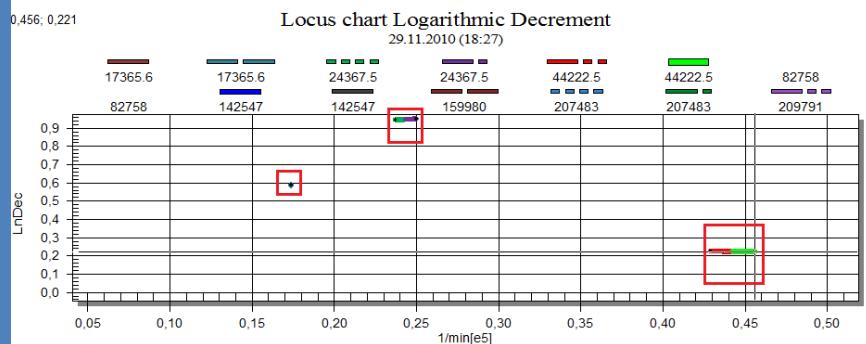
$k_2 = 0.5e +8 \text{ H/m}$

17358.2 (289.3)
17373.0 (289.6)
24106.4 (401.8)
24637.3 (410.6)
43213.1 (720.2)
45303.1 (755.1)



Forced oscillations of the rotor supported by AMB

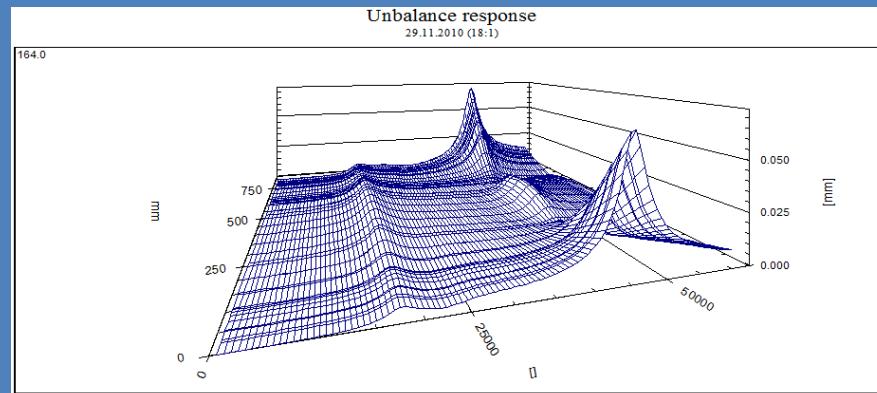
Locus chart of logarithmic decrements



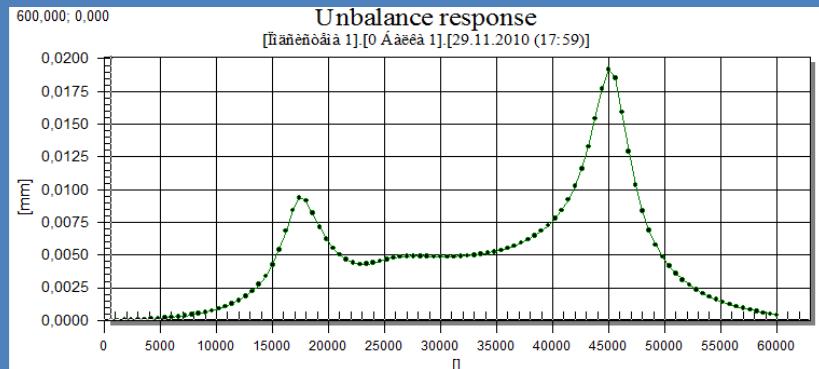
Distribution of deformations potential energy

Узел	Критические частоты вращения, об/мин		
	17373	24637	45303
Вал ротора	15.506	3.843	87.558
АМП ₁	48.745	43.710	3.602
АМП ₂	35.749	52.447	8.839
Сумма	100	100	100

3D - amplitude-frequency rotor response

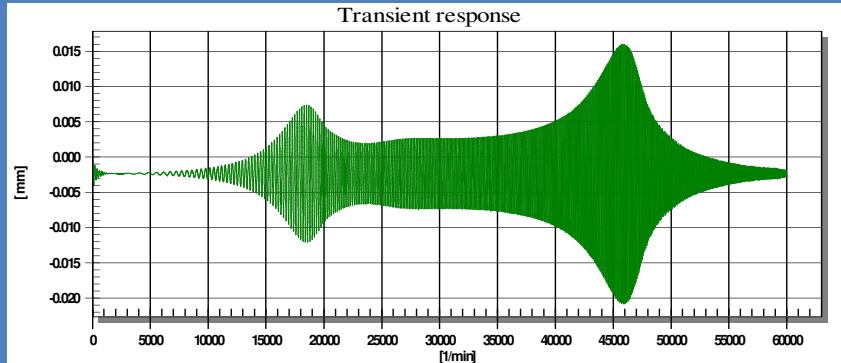


2D - amplitude-frequency rotor response.
The AMP₁ section

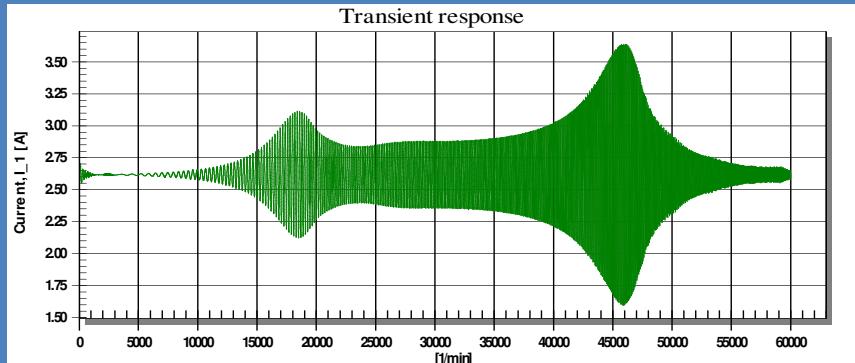


Unsteady analysis of the rotor supported by AMB

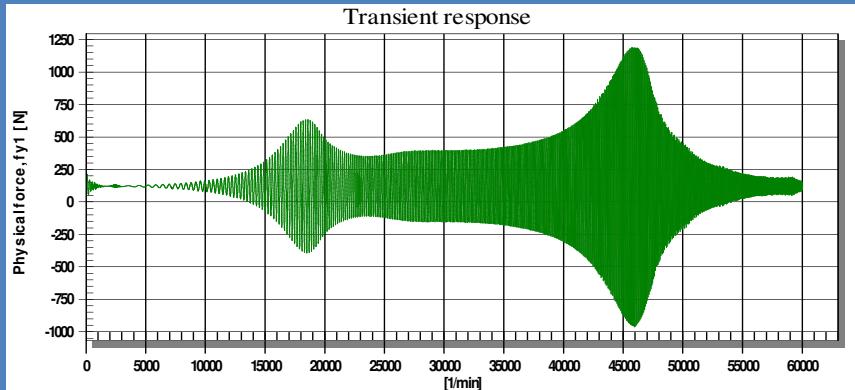
Unsteady analysis in consideration of weight,
 $K=0.5 \text{ e}+8 =\text{const}$



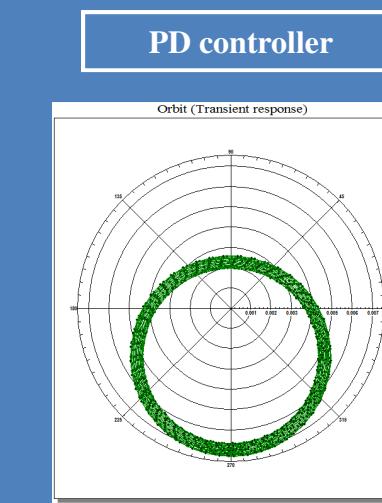
Change in current, $I_{\text{пред}} = 5 \text{ A}$



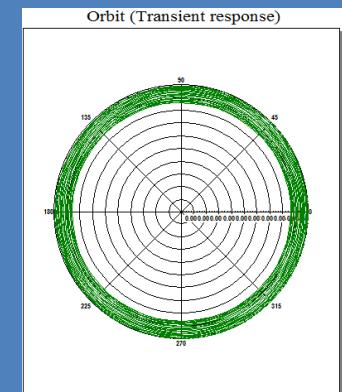
Reactions in support



Motion orbits, AMB_1 section

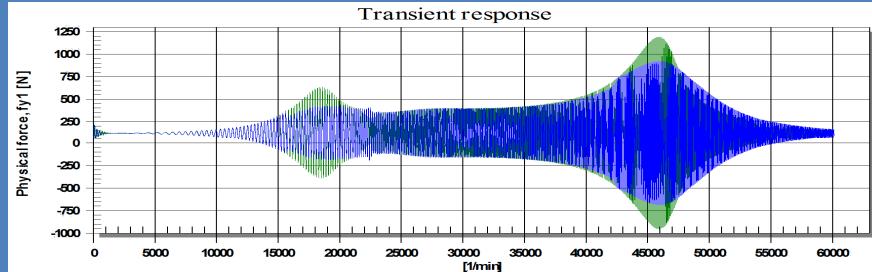
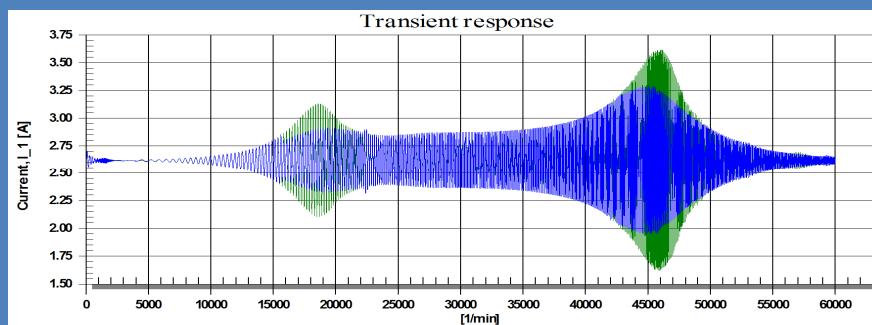
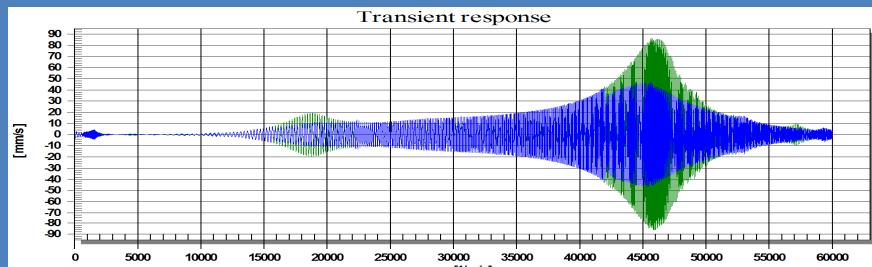
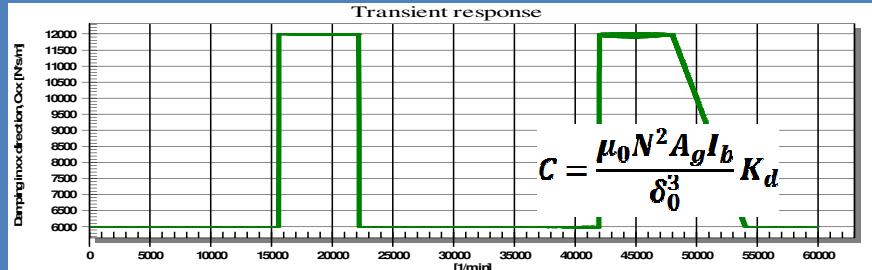


PID controller

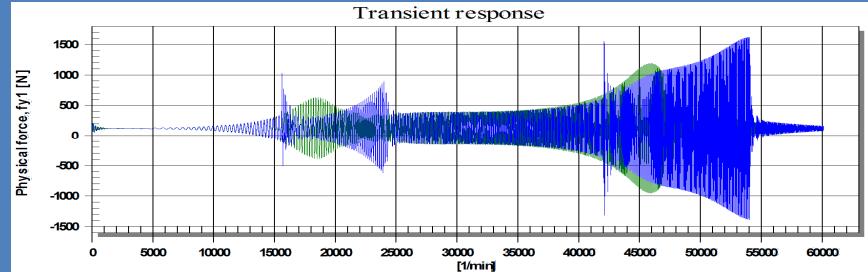
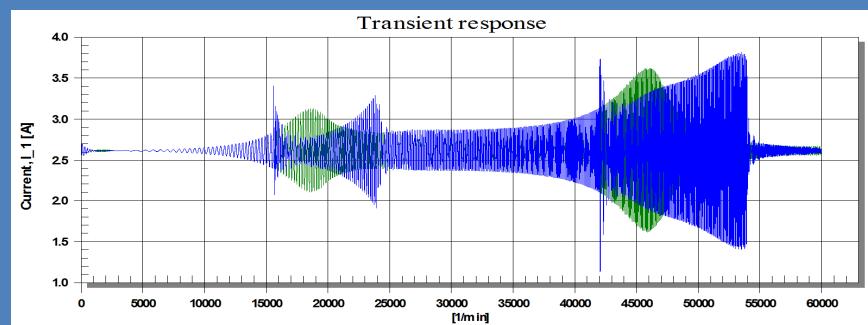
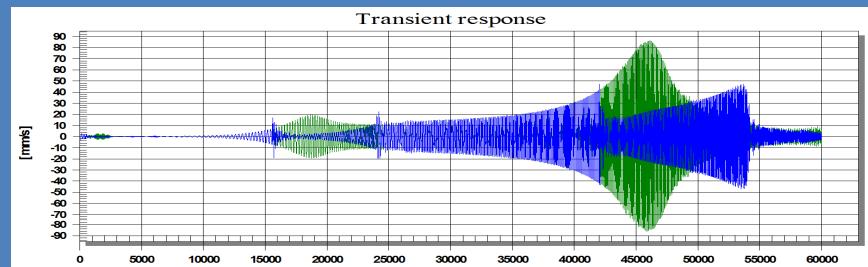
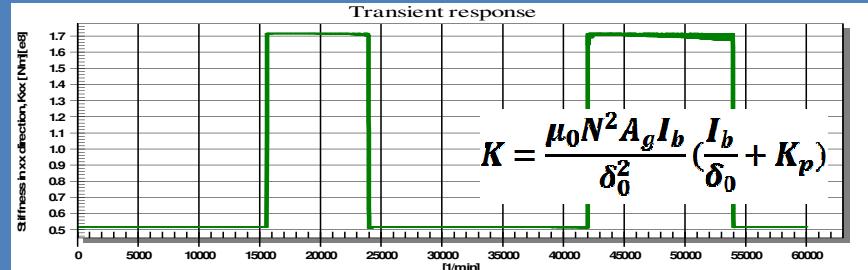


AMB stiffness and damping control

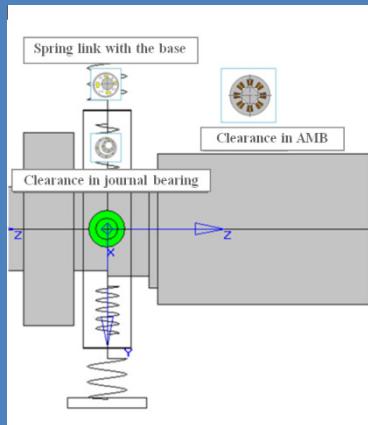
AMB damping control



AMB stiffness control



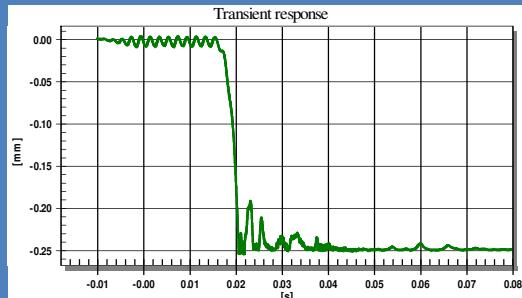
The rotor dropdown on the journal bearings



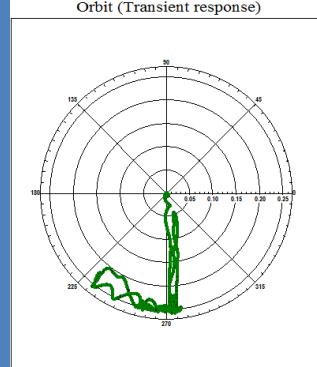
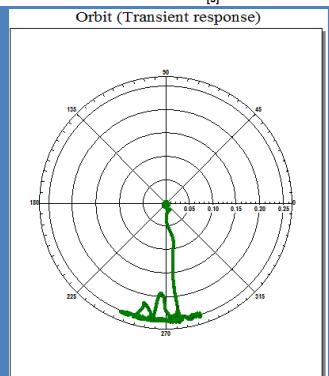
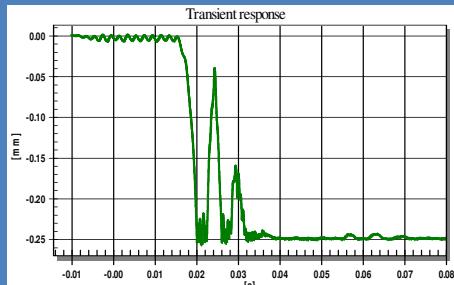
Radial clearance in AMB , mm	0.5
Radial clearance in journal bearing, mm	0.25
AMB stiffness, N/m	0.5e+8
AMB damping, N s/m	6000
Contact stiffness, N/m	1e+10

μ (Steel on babbitt) 0.005

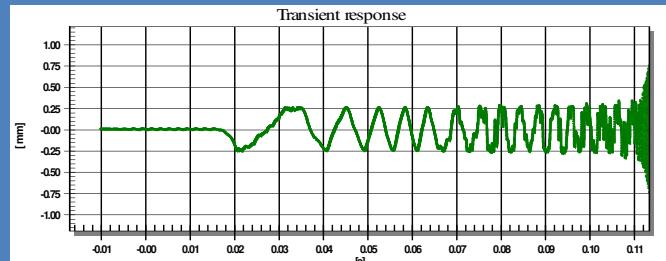
Journal bearing 1



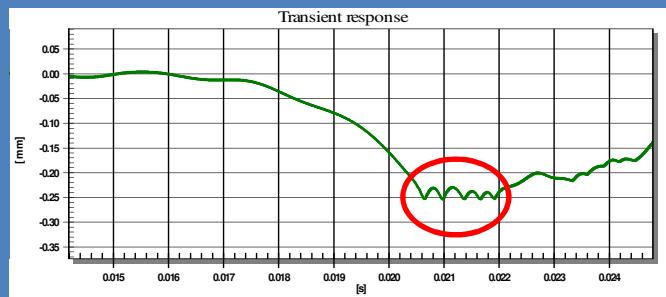
Journal bearing 2



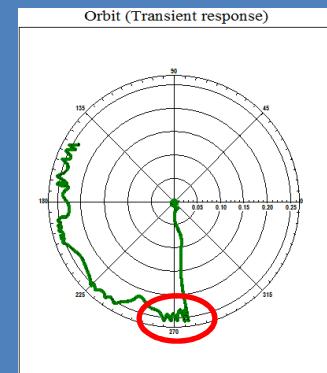
μ (Steel on graphit) 0.1



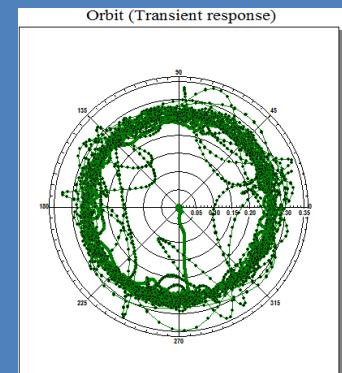
Transition period



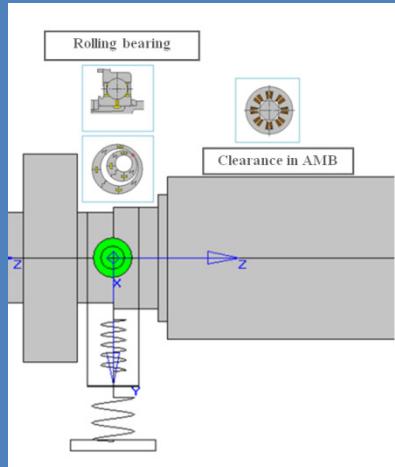
Going into
backward precession



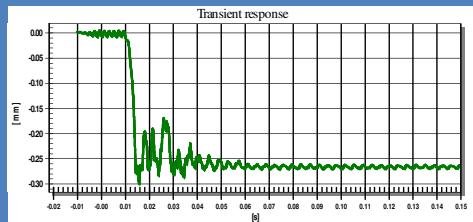
Backward precession



The rotor dropdown on the rolling bearings

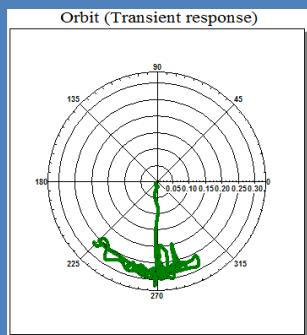
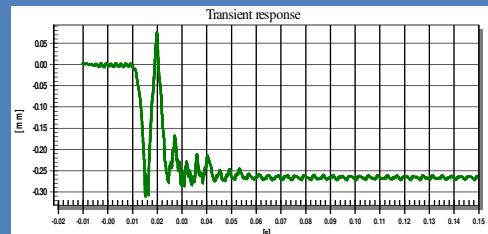


Bearing 1

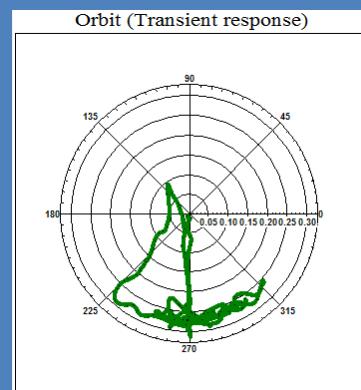


Radial clearance in AMB , mm	0.5
Radial clearance in rolling bearing, mm	0
Radial clearance between the shaft and the rolling bearing, mm	0.25
AMB stiffness, N/m	0.5e+8
AMB damping, N s/m	6000
Contact stiffness in rolling bearing, N/m	1e+10

Bearing 2

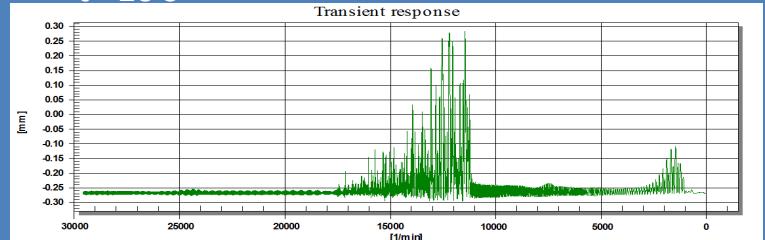


Rotating speed of
inner ring of rolling
bearing
 $n = 30000$ rpm

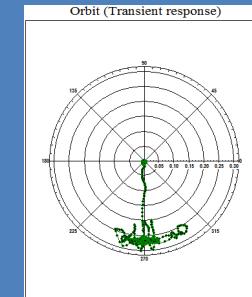


The rotor stop.

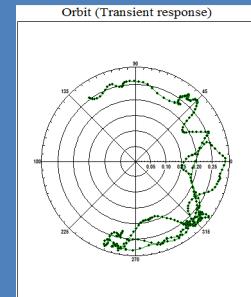
Rotating speed changes from $n = 30000$ rpm
up to $n = 0$ rpm
 $\Delta t = 10$ s



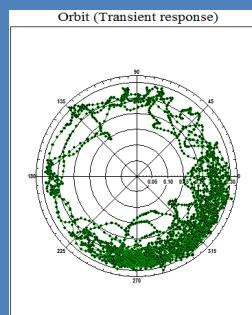
Movement before
whirling motion



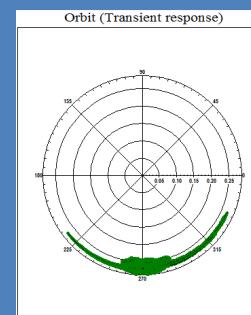
Going into
whirling motion



Full-clearance motion



Following stop



The general methodology of designing the rotor supported by AMB



Determination of necessary values of AMB stiffness and damping

Estimation of AMB control coefficients and adjustment of the control system

Determination of the rotor's damped critical speeds and mode shapes – places of prospective resonances

Calculation of forced oscillations and amplitude values of vibroparameters : displacements, vibrovelocity, reactions in supporting units. etc.

Development of the program of current – AMB stiffness and damping – control for passing systems resonances and going into the operating range

Unsteady analysis of the rotor supported by AMB with the aim of more precise definition of the rotor's characteristics at transient regimes

Simulation of the rotor supported by backup bearings. The non-linear unsteady rotor analysis. The aim is to determine the possibility of the rotor's going into whirling motion or backward precession

The unsteady rotor analysis after switching off AMB supported by non-linear rolling bearings while the rotor's deceleration and determination of resonance regimes

**THANK YOU FOR
YOUR ATTENTION!**